Neutrino Oscillation Workshop (NOW 2018) Rosa Marina, Ostuni, Italy, September 9-16, 2018



Neutrinoless double-beta decay: Theory challanges Fedor Šimkovic







OUTLINE

I. Introduction Majorana, Pontecorvo, Weinberg **II.** The 0*ν*ββ-decay scenarios due neutrinos exchange (simpliest, sterile v, LR-symmetric model, interpolating *formula*) **III.** DBD NMEs – Current status (deformed QRPA versus ISM, ...) **IV.** Is there a proportionality between $0\nu\beta\beta$ - and $2\nu\beta\beta$ -decay NMEs? (role of SU(4) symmetry ...) **V.** New modes of the double-beta decay with emission of a single electron from an atom **VI.** Conclusion

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I. Introduction

Majorana fermion



https://en.wikipedia.org/wiki/File:Ettore_Majorana.jpg



CNNP 2018, Catania, October 15-21, 2018

TEORIA SIMMETRICA DELL'ELETTRONE E DEL POSITRONE

Nota di ETTORE MAJORANA

Symmetric Theory of Electron and Positron Nuovo Cim. 14 (1937) 171

Sunto. - Si dimostra la possibilità di pervenire a una piena simmetrizzasione formale della teoria quantistica dell'elettrone e del positrone facendo uso di un nuovo processo di quantizzazione. Il significato delle equazioni di DIRAC ne risulta alquanto modificato e non vi è più luogo a parlare di stati di energia negativa; nè a presumere per ogni altro tipo di particelle, particolarmente neutre, l'esistenza di « antiparticelle » corrispondenti ai « vuoti » di energia negativa.

L'interpretazione dei cosidetti « stati di energia negativa » proposta da DIRAC (¹) conduce, come è ben noto, a una descrizione sostanzialmente simmetrica degli elettroni e dei positroni. La sostanziale simmetria del formalismo consiste precisamente in questo, che fin dove è possibile applicare la teoria girando le difficoltà di convergenza, essa fornisce realmente risultati del tutto simmetrici. Tuttavia gli artifici suggeriti per dare alla teoria una forma simmetrica

che si accord sia perchè s perchè la sir procedimenti bilmente dov

trica, sia iante tali che possinuova via

isfacenti ;

che conduce più direttamente alla meta.

Per quanto riguarda gli elettroni e i positroni, da essa si può veramente attendere soltanto un progresso formale; ma ci sembra importante, per le possibili estensioni analogiche, che venga a cadere la nozione stessa di stato di energia negativa. Vedremo infatti che è perfettamente possibile costruire, nella maniera più naturale, una teoria delle particelle neutre elementari senza stati negativi.

9/14/2018

Fedor Si

(4) P. A. M. DIRAC, & Proc. Camb. Phil. Soc. 5, 80, 150, 1924. V. anche W. HEISENBERG, & ZS. f. Phys. 5, 90, 209, 1934.



 $\nu \leftrightarrow \overline{\nu}$ oscillation (neutrinos are Majorana particles)

MESONIUM AND ANTIMESONIUM

B. PONTECORVO

Joint Institute for Nuclear Research

Submitted to JETP editor May 23, 1957

J. Exptl. Theoret. Phys. (U.S.S.R.) 33, 549-551 (August, 1957)

INVERSE BETA PROCESSES AND NONCON-SERVATION OF LEPTON CHARGE

B. PONTECORVO

Joint Institute for Nuclear Research

Submitted to JETP editor October 19, 1957

J. Exptl. Theoret. Phys. (U.S.S.R.) 34, 247-249 (January, 1958)



It follows from the above assumptions that in vacuum a neutrino can be transformed into an antineutrino and vice versa. This means that the neutrino and antineutrino are "mixed" particles, i.e., a symmetric and antisymmetric combination of two truly neutral Majorana particles ν_1 and ν_2 of different combined parity.⁵

1968 Gribov, Pontecorvo [PLB 28(1969) 493] oscillations of neutrinos - a solution of deficit of solar neutrinos in Homestake exp.



After 62 years we know

Fundamental V properties

No answer yet

3 families of light (V-A) neutrinos: ν_e, ν_µ, ν_τ
ν are massive: we know mass squared differences
relation between flavor states and mass states (neutrino mixing)



- Are v Dirac or Majorana?
- •Is there a CP violation in v sector?
- Are neutrinos stable?
- What is the magnetic moment of v?
- Sterile neutrinos?
- Statistical properties of v? Fermionic or partly bosonic?



Currently main issue

Nature, Mass hierarchy, CP-properties, sterile v



The observation of neutrino oscillations has opened a new excited era in neutrino physics and represents a big step forward in our knowledge of neutrino properties



Beyond the Standard model physics (EFT scenario)



The absence of the righthanded neutrino fields in the SM is the simplest, most economical possibility. In such a scenario Majorana mass term is the only possibility for neutrinos to Be massive and mixed. This mass term is generated by the Lepton number violating Weinberg effective Lagrangian.

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 $\mathcal{L} = \mathcal{L}_{SM}^{(4)} +$

Beyond the SM physics

 $rac{1}{\Lambda}\sum c_i^{(5)}\mathcal{O}_i^{(5)}+rac{1}{\Lambda^2}\sum c_i^{(6)}\mathcal{O}_i^{(6)}+\mathcal{O}(rac{1}{\Lambda^3})$

CERNCOURSER

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Weinberg, 1979: d=5

 $0\nu\beta\beta$ decay:



 $\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H) (L_j H)$

. Weinberg does not take credit for

predicting neutrino masses, but he thinks it's the right interpretation. What's more, he says, the non-renormalisable interaction that produces the neutrino masses is probably also accompanied with non-renormalisable interactions that produce proton decay and other things that haven't been observed, such as violation of baryon-number conservations. "We don't know anything about the details of those terms, but I'll swear they are there."

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Amplitude for (A,Z)→(A,Z+2)+2e⁻ can be divided into:

M. Hirsch, Pontecorvo school 2015

mass mechanism: d=5



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$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H) (L_j H)$$

Weinberg, 1979

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long range: d=7

+



 $\mathcal{O}_2 \propto LLLe^c H$ $\mathcal{O}_3 \propto LLQd^c H$ $\mathcal{O}_4 \propto LL\bar{Q}\bar{u}^c H$ $\mathcal{O}_8 \propto L\bar{e}^c \bar{u}^c d^c H$

Babu, Leung: 2001 de Gouvea, Jenkins: 2007

short range: d=9 (d=11)



 $\mathcal{O}_{5} \propto LLQd^{c}HHH^{\dagger}$ $\mathcal{O}_{6} \propto LL\bar{Q}\bar{u}^{c}HH^{\dagger}H$ $\mathcal{O}_{7} \propto LQ\bar{e}^{c}\bar{Q}HHH^{\dagger}$ $\mathcal{O}_{9} \propto LLLe^{c}Le^{c}$ $\mathcal{O}_{10} \propto LLLe^{c}Qd^{c}$ $\mathcal{O}_{11} \propto LLQd^{c}Qd^{c}$

Physics at LHC(Jose Valle talk)





If $0\nu\beta\beta$ is observed the ν is a Majorana particle

II. Different $0\nu\beta\beta$ -decay scenarios



I.a. The simplest 0 vββ-decay scenario: LHC & LNV scale A is too large

$$\mathcal{L}_{5}^{eff} = -\frac{1}{\Lambda} \sum_{l_{1}l_{2}} \left(\overline{\Psi}_{l_{1}L}^{lep} \tilde{\Phi} \right) \acute{Y}_{l_{1}l_{2}} \left(\tilde{\Phi}^{T} (\Psi_{l_{2}L}^{lep})^{c} \right)$$

Heavy Majorana leptons $N_i (N_i=N_i^c)$ singlet of $SU(2)_L xU(1)_Y$ group Yukawa lepton number violating int.

$$egin{array}{cccc} oldsymbol{\mathcal{V}} & oldsymbol{\mathcal{V}} & oldsymbol{\mathcal{V}} & oldsymbol{\mathcal{H}}^0 & oldsymbol{H}^0 & oldsymbol{H}^0 & oldsymbol{H}^0 & oldsymbol{H}^0 & oldsymbol{H}^0 & oldsymbol{\mathcal{V}} & oldsymbol{\mathcal{V}}_{
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$$m_i = rac{v}{\Lambda} (y_i v), \quad i = 1, 2, 3$$
 $\Lambda \ge 10^{15} \, \mathrm{GeV}$

S.M. Bilenky, Phys.Part.Nucl.Lett. 12 (2015) 453-461

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The three Majorana neutrino masses are suppressed by the ratio of the electroweak scale and a scale of a lepton-number violating physics.

The discovery of the $\beta\beta$ -decay and absence of transitions of flavor neutrinos into sterile states would be evidence in favor of this minimal scenario.

 $(A,Z) \rightarrow (A,Z+2) + e^- + e^-$

 $\left(T^{0\nu}_{1/2}\right)^{-1} = \left|\frac{m_{\beta\beta}}{m_e}\right|^2 g_A^4 \left|M^{0\nu}_{\nu}\right|^2 G^{0\nu}$

	_ A=const (even) _	transition	$G^{01}(E_0, Z)$	$Q_{\beta\beta}$	Abund.	$ M^{0\nu} ^2$
nits)			$ imes 10^{14} y$	[MeV]	(%)	
Atomic mass (arbitrary u	Z odd Z	$^{150}Nd \rightarrow ^{150}Sm$	26.9	3.667	6	?
		${}^{48}Ca \rightarrow {}^{48}Ti$	8.04	4.271	0.2	?
	$ \land \land$	${}^{96}Zr \rightarrow {}^{96}Mo$	7.37	3.350	3	?
		$^{116}Cd \rightarrow {}^{116}Sn$	6.24	2.802	7	?
	$ \downarrow \downarrow $	$^{136}Xe \rightarrow {}^{136}Ba$	5.92	2.479	9	?
	Γ / [•] β β / Ι	$^{100}Mo \rightarrow {}^{100}Ru$	5.74	3.034	10	?
		$^{130}Te \rightarrow ^{130}Xe$	5.55	2.533	34	?
		$^{82}Se \rightarrow {}^{82}Kr$	3.53	2.995	9	?
-2	2 -1 0 +1 +2	$^{76}Ge \rightarrow {}^{76}Se$	0.79	2.040	8	?
	$\Delta Z = Z - Z_0$					

The NMEs for $0\nu\beta\beta$ -decay must be evaluated using tools of nuclear theory

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Effective mass of Majorana neutrinos





Nuclear medium effect on the light neutrino mass exchange mechanism of the Ονββ-decay

S.G. Kovalenko, M.I. Krivoruchenko, F. Š., Phys. Rev. Lett. 112 (2014) 142503



Mean field:
$$\overline{q}q \rightarrow \langle \overline{q}q \rangle$$
and $\langle \overline{q}q \rangle \approx 0.5 \langle q^{\dagger}q \rangle \approx 0.25 \, \mathrm{fm}^{-3}$ The effect depends on $\langle \chi \rangle = -\frac{g_{\chi}}{m_{\chi}^2} \langle \overline{q}q \rangle$ A comparison with \mathbf{G}_{F} :Typical scale: $\langle \chi \rangle g_{ij}^a = -\frac{G_F}{\sqrt{2}} \langle \overline{q}q \rangle \varepsilon_{ij}^a \approx -25 \varepsilon_{ij}^a \, \mathrm{eV}$ $\frac{g_{\chi}g_{ij}^a}{m_{\chi}^2} = \frac{G_F}{\sqrt{2}} \varepsilon_{ij}^a$ We expect: $25 \varepsilon_{ij}^a < 1 \rightarrow m_{\chi}^2 > 25 \frac{g_{\chi}g_{ij}^a \sqrt{2}}{G_F} \sim 1 \, \mathrm{TeV}^2$ Universal scalar interaction $g_{ij}^a = \delta_{ij}g_a$ $\varepsilon_{ij}^a = \delta_{ij}\varepsilon_a$

In medium effective Majorana v mass

$$m_{\beta\beta} = \sum_{i=1}^{n} U_{ei}^{2} \xi_{i} \frac{\sqrt{(m_{i} + \langle \chi \rangle g_{1})^{2} + (\langle \chi \rangle g_{2})^{2}}}{(1 - \langle \chi \rangle g_{4})^{2}}.$$

Complementarity between β -decay, $0\nu\beta\beta$ –decay and cosmological measurements might be spoiled





Left-handed neutrinos: Majorana neutrino mass eigenstate N with arbitrary mass m_N

Faessler, Gonzales, Kovalenko, F. Š., PRD 90 (2014) 096010]

$$[T_{1/2}^{0\nu}]^{-1} = G^{0\nu}g_{\rm A}^4 \left| \sum_{\rm N} \left(U_{e\rm N}^2 m_{\rm N} \right) m_{\rm p} M'^{0\nu}(m_{\rm N}, g_{\rm A}^{\rm eff}) \right|^2$$

General case

$$M'^{0\nu}(m_{\rm N}, g_{\rm A}^{\rm eff}) = \frac{1}{m_{\rm p}m_{\rm e}} \frac{R}{2\pi^2 g_{\rm A}^2} \sum_n \int d^3x \, d^3y \, d^3p \qquad M'^{0\nu}(m_{\rm N} \to 0, g_{\rm A}^{\rm eff}) = \frac{1}{m_{\rm p}m_{\rm e}} M'^{0\nu}_{\nu}(g_{\rm A}^{\rm eff})$$

$$\times e^{i\mathbf{p}\cdot(\mathbf{x}-\mathbf{y})} \frac{\langle 0_F^+ | J^{\mu\dagger}(\mathbf{x}) | n \rangle \langle n | J^{\dagger}_{\mu}(\mathbf{y}) | 0_I^+ \rangle}{\sqrt{p^2 + m_N^2} (\sqrt{p^2 + m_N^2} + E_n - \frac{E_I - E_F}{2})} M'^{0\nu}(m_{\rm N} \to \infty, g_{\rm A}^{\rm eff}) = \frac{1}{m_{\rm N}^2} M'^{0\nu}_{\rm N}(g_{\rm A}^{\rm eff})$$
heavy v exchange

Particular cases

$$\begin{split} [T_{1/2}^{0\nu}]^{-1} &= G^{0\nu} g_{\mathrm{A}}^{4} \times \\ &\times \begin{cases} \left| \frac{\langle m_{\nu} \rangle}{m_{\mathrm{e}}} \right|^{2} \left| M_{\nu}^{\prime 0\nu}(g_{\mathrm{A}}^{\mathrm{eff}}) \right|^{2} & \text{for } m_{\mathrm{N}} \ll p_{\mathrm{F}} \\ \left| \langle \frac{1}{m_{\mathrm{N}}} \rangle m_{\mathrm{p}} \right|^{2} \left| M_{\mathrm{N}}^{\prime 0\nu}(g_{\mathrm{A}}^{\mathrm{eff}}) \right|^{2} & \text{for } m_{\mathrm{N}} \gg p_{\mathrm{F}} \end{cases} \begin{pmatrix} \langle m_{\nu} \rangle = \sum_{\mathrm{N}} U_{\mathrm{eN}}^{2} m_{\mathrm{N}} \\ \left| \langle \frac{1}{m_{\mathrm{N}}} \rangle m_{\mathrm{p}} \right|^{2} \left| M_{\mathrm{N}}^{\prime 0\nu}(g_{\mathrm{A}}^{\mathrm{eff}}) \right|^{2} & \text{for } m_{\mathrm{N}} \gg p_{\mathrm{F}} \end{split}$$

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Faessler, Gonzales, Kovalenko, F. Š., PRD 90 (2014) 096010]





Exclusion plot in |U_{eN}|² – m_N plane $T^{0v}_{1/2}(^{76}Ge) \ge 3.0 \ 10^{25} \text{ yr}$ $T^{0v}_{1/2}(^{136}Xe) \ge 3.4 \ 10^{25} \text{ yr}$



Improvements: i) QRPA (constrained Hamiltonian by $2\nu\beta\beta$ half-life, self-consistent treatment of src, restoration of isospin symmetry ...), ii) More stringent limits on the $0\nu\beta\beta$ half-life

II.c. The 0vββ-decay within L-R symmetric theories (interpolating formula)

(D-M mass term, see-saw, V-A and V+A int., exchange of heavy neutrinos)

A. Babič, S. Kovalenko, M.I. Krivoruchenko, F.Š., PRD 98, 015003 (2018)

$$[T_{1/2}^{0\nu}]^{-1} = \eta_{\nu N}^2 C_{\nu N} \qquad \qquad C_{\nu N} = g_A^4 \left| M_{\nu}^{\prime 0\nu} \right|^2 G^{0\nu}$$

Mixing of light and heavy neutrinos

$$\mathcal{U} = \left(egin{array}{cc} m{U} & m{S} \ T & m{V} \end{array}
ight)$$

$$\boldsymbol{\nu_{eL}} = \sum_{j=1}^{3} \left(\boldsymbol{U_{ej}} \nu_{jL} + S_{ej} (N_{jR})^C \right)$$
$$\boldsymbol{\nu_{eR}} = \sum_{j=1}^{3} \left(T_{ej}^* (\nu_{jL})^C + \boldsymbol{V_{ej}^*} N_{jR} \right)$$

. n

Effective LNV parameter within LRS model

$$\eta_{\nu N}^{2} = \left| \sum_{j=1}^{3} \left(U_{ej}^{2} \frac{m_{j}}{m_{e}} + S_{ej}^{2} \frac{\langle p^{2} \rangle_{a}}{\langle p^{2} \rangle_{a} + M_{j}^{2}} \frac{M_{j}}{m_{e}} \right) \right|^{2} + \lambda^{2} \left| \sum_{j=1}^{3} \left(T_{ej}^{2} \frac{m_{j}}{m_{e}} + V_{ej}^{2} \frac{\langle p^{2} \rangle_{a}}{\langle p^{2} \rangle_{a} + M_{j}^{2}} \frac{M_{j}}{m_{e}} \right) \right|^{2}$$

6x6 PMNS see-saw v-mixing matrix (the most economical one)

6x6 neutrino mass matrix

6x6 matrix: 15 angles, 10+5 CP phases 3x3 matrix: 3 angles, 1+2 CP phases

3x3 block matrices U, S, T, V are generalization of PMNS matrix

Assumptions:

i) the see-saw structure

ii) mixing between different generations is neglected

$$\mathcal{U}_{ ext{PMNS}} \;=\; \left(egin{array}{ccc} U_{ ext{PMNS}} & \zeta \; \mathbf{1} \ -\zeta \; \mathbf{1} & U_{ ext{PMNS}}^{\dagger} \end{array}
ight) \; egin{array}{ccc} \mathcal{U}_{ ext{PMNS}} & \mathcal{U}_{ ext{PMNS}} = \mathcal{U}_{ ext{PMNS}}^{\dagger} \; \mathcal{U}_{ ext{PMNS}} = \mathbf{1} \ \mathcal{U}_{ ext{PMNS}} & \mathcal{U}_{ ext{PMNS}} \end{array}
ight)$$

see-saw parameter $\zeta = \frac{m_{\rm D}}{m_{\rm LNV}}$ 6x6 matrix: 3 angles, 1+2 CP phases, 1 see-saw par.

6x6 PMNS see-saw v-mixing matrix $\mathcal{U} = \begin{pmatrix} U_0 & \zeta \mathbf{1} \\ -\zeta \mathbf{1} & V_0 \end{pmatrix}$ (the most economical one)

$$U_{0} = U_{\text{PMNS}}$$
A. Babič, S. Kovalenko, M.I. Krivoruchenko, F.Š., PRD 98, 015003 (2018)

$$V_{0} = U_{\text{PMNS}}^{\dagger} = \begin{pmatrix} c_{12} c_{13} e^{-i\alpha_{1}} & (-s_{12} c_{23} - c_{12} s_{13} s_{23} e^{-i\delta}) e^{-i\alpha_{1}} & (s_{12} s_{23} - c_{12} s_{13} c_{23} e^{-i\delta}) e^{-i\alpha_{1}} \\ s_{12} c_{13} e^{-i\alpha_{2}} & (c_{12} c_{23} - s_{12} s_{13} s_{23} e^{-i\delta}) e^{-i\alpha_{2}} & (-c_{12} s_{23} - s_{12} s_{13} c_{23} e^{-i\delta}) e^{-i\alpha_{2}} \\ s_{13} e^{i\delta} & c_{13} s_{23} & c_{13} c_{23} \end{pmatrix}$$

Assumption about heavy neutrino masses M_i (by assuming see-saw)

 $m_i M_i \simeq m_D^2$ **Inverse** proportional **Proportional**

Heavy Majorana mass $M^{R}_{\beta\beta}$ depends on the "Dirac" CP violating phase δ^{-6}

Contribution from exchange of heavy neutrino to $0\nu\beta\beta$ -decay rate might be large





A. Babič, S. Kovalenko, M.I. Krivoruchenko, F.Š., PRD 98, 015003 (2018)

II.d. The 0vββ-decay within L-R symmetric theories (*D-M mass term, see-saw, V-A and V+A int., exchange of light neutrinos*)



Mixing of ligt and heavy neutrinos $\nu_{eL} = \sum_{j=1}^{3} \left(U_{ej} \nu_{jL} + S_{ej} (N_{jR})^C \right),$ $\nu_{eR} = \sum_{j=1}^{3} \left(T_{ej}^* (\nu_{jL})^C + V_{ej}^* N_{jR} \right)$

> Effective LNV parameter due to RHC

$$\langle \lambda
angle \; = \; \lambda \mid \sum_{j=1}^{3} U_{ej} T_{ej}^{*}$$

 \mathbf{a}

Ratio of masses of vector bosons

 $\lambda = (M_{W_1}/M_{W_2})^2$

$m_{\beta\beta}$ and λ mechanisms



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F.Š., R. Dvornický, R. Štefánik, Found. Phys. 5, 57 (2017)

30

 $m_{\beta\beta} = 50 \text{ meV} (136 \text{ Xe}), g_A = 1.269, QRPA \text{ NMEs}$



III. 0 νββ decay NMEs

0vββ-decay NME (light v mass) – status 2017

J. Engel, J. Menendez, Rept. Prog. Phys. 80, 046301 (2017)





Suppression of the $0\nu\beta\beta$ -decay NMEs due to different deformation of initial and final nuclei



Systematic study of the deformation effect on the 2νββ-decay NME within deformed QRPA

Alvarez, Sarriguren, Moya, Pacearescu, Faessler, F.Š., Phys. Rev. C 70 (2004) 321

The suppression of the NME depends on the relative deformation of initial and final nuclei

F.Š., Pacearescu, Faessler, NPA 733 (2004) 321



0vββ-decay NMEs within deformed QRPA with partial restoration of isospin symmetry (light neutrino exchange)

D. Fang, A. Faessler, F.Š., PRC 97, 045503 (2018)





Ab Initio Nuclear Structure (Often starts with chiral effective-field theory)

Nucleons, pions sufficient below chiral symmetry breaking scale. Expansion of operators in power of Q/Λ_{γ} . $Q=m_{\pi}$ or typical nucleon momentum.



Supporting nuclear physics experiments (2νββ-decay ChER, pion and heavy ion DCX, nucleon transfer reactions etc)

$$^{18}O + {}^{40}Ca \rightarrow {}^{18}F + {}^{40}K \rightarrow {}^{18}Ne + {}^{40}Ar$$

Heavy ion DCX: NUMEN (LNC-INFN), HIDCX (RCNP/RIKEN) H. Lenske group Theory of heavy ion DCX and Connection to DBD NMEs

Double GT Giant resonances (exhausts a major part of sum-rule strength)



E_x in grand-daughter nucleus

V. Is there a proportionality between 0vββ- and 2vββ-decay NMEs? Understanding of the $2\nu\beta\beta$ -decay NMEs is of crucial importance for correct evaluation of the $0\nu\beta\beta$ -decay NMEs

$$(A,Z) \rightarrow (A,Z+2) + 2e^- + 2\overline{\nu}_e$$

Both 2νββ and 0νββ operators connect the same states. Both change two neutrons into two protons.

Explaining 2νββ-decay is necessary but not sufficient

There is no reliable calculation of the 2 νββ-decay NMEs

Calculation via intermediate nuclear states: **QRPA** (sensitivity to pp-int.) **ISM** (quenching, truncation of model space, spin-orbit partners)

Calculation via closure NME: IBM, PHFB

No calculation: EDF

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ISM: N. Shimizu, J. Menendez, K. Yako, PRL 120, 142502 (2018)

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	$M^{DGT}=M^{2\nu}_{GT}$								
	SSD ChER								
	⁴⁸ Ca 0.22								
	⁷⁶ Ge 0.52								
	⁹⁶ Zr 0.22								
	¹⁰⁰ Mo 0.35								
	¹¹⁶ Cd 0.35 0.30								
	¹²⁸ Te 0.41								
	EDF: $0.6 \rightarrow 1.2$								
	ISM: $0.1 \rightarrow 0.7$								
	IBM: $1.6 \rightarrow 4.4$								
	QRPA: $ 0.1 \rightarrow 0.7 $								
IBM: J. Barea, J. Kotila, F. Iachello, PRC 91, 034304 (2015)									
QRPA: F.Š., R. Hodák, A. Faessler, P. Vogel, PRC 83, 015502 (2011)									
	M ^{DGT} – only 1+								
	M^{0v} - contribution								

from many $J^{\pi}(!)$

QRPA: There is no proportionality between 0νββ-decay and 2νββ-decay NMEs



Region of GT resonance



r- *relative distance of two decaying nucleons*

Neutrino potential prefers short distances







QRPA – SU(4) prametrization



 $2\nu\beta\beta$ -decay within the QRPA (restoration of the SU(4) symmetry – M²ⁿ_{cl} =0)

$$\begin{array}{rcl} g_A^{\text{eff}} &=& q \times g_A^{\text{free}} = 0.901 \\ g_A^{\text{free}} &=& 1.269, \quad q = 0.710 \end{array}$$

Nucleus	d_{pp}^i	d_{pp}^f	d_{nn}^i	d_{nn}^f	$g_{pp}^{T=1}$	$g_{pp}^{T=0}$	$M_F^{2\nu}$	$M_{GT}^{2\nu} \times q^2$	$M_{exp}^{2\nu}$
							$[MeV^{-1}]$	$[MeV^{-1}]$	$[MeV^{-1}]$
^{48}Ca	-	1.069	-	0.982	1.028	0.745	-0.003	0.037	0.046
$^{76}\mathrm{Ge}$	0.922	0.960	1.053	1.085	1.021	0.733	0.003	0.076	0.136
82 Se	0.861	0.921	1.063	1.108	1.016	0.737	0.001	0.070	0.100
$^{96}\mathrm{Zr}$	0.910	0.984	0.752	0.938	0.961	0.739	0.001	0.161	0.097
^{100}Mo	1.000	1.021	0.926	0.953	0.985	0.799	-0.001	0.304	0.251
^{116}Cd	0.998	-	0.934	0.890	0.892	0.877	-0.000	0.059	0.136
$^{128}\mathrm{Te}$	0.816	0.857	0.889	0.918	0.965	0.741	0.017	0.075	0.052
$^{130}\mathrm{Te}$	0.847	0.922	0.971	1.011	0.963	0.737	0.016	0.064	0.037
$^{136}\mathrm{Xe}$	0.782	0.885	-	0.926	0.910	0.685	0.014	0.039	0.022



V. Quenching of g_A

Quenching in nuclear matter: $g^{eff}_{A} = q g^{free}_{A}$ (from theory: $T_{1/2}^{0n}$ up 50 x larger)



g_v =1 inside nuclei

 g^{free} =1.27 at the nucleon level g^{eff}_A = ? inside nuclei

ISM: $(g^{eff}_{A})^4 \simeq 0.66 \ ({}^{48}Ca), 0.66 \ ({}^{76}Ge), 0.30 \ ({}^{76}Se), 0.20 \ ({}^{130}Te) \text{ and } 0.11 \ ({}^{136}Xe)$ **IBM:** $(g_{A}^{eff})^4 \simeq (1.269 \text{ A}^{-0.18})^4 = 0.063$ 53 **ORPA:** $(g^{eff})^4 = 0.30$ and 0.50 for ¹⁰⁰Mo and ¹¹⁶Cd



Faessler, Fogli, Lisi, Rodin, Rotunno, F. Š, J. Phys. G 35, 075104 (2008).

 $(g^{eff}_{A})^4 = 0.30$ and 0.50 for ¹⁰⁰Mo and ¹¹⁶Cd, respectively (The QRPA prediction). g^{eff}_{A} was treated as a completely free parameter alongside g_{pp} (used to renormalize particl-particle interaction) by performing calculations within the QRPA and RQRPA. It was found that a least-squares fit of g_{A}^{eff} and g_{pp} , where possible, to the β -decay rate and β +/EC rate of the J = 1⁺ ground state in the intermediate nuclei involved in double-beta decay in addition to the $2\nu\beta\beta$ rates of the initial nuclei, leads to an effective geff_A of about 0.7 or 0.8.





Extended calculation also for neighbor isotopes performed by

F.F. Depisch and J. Suhonen, PRC 94, 055501 (2016)

Quenching of g_A -IBM ($T_{1/2}^{0n}$ suppressed up to factor 50)

 $(g^{eff}{}_{A})^{4} \simeq (1.269 \text{ A}^{-0.18})^{4} = 0.063$ (The Interacting Boson Model). This is an incredible result. The quenching of the axial-vector coupling within the IBM-2 is more like 60%.

It has been determined by theoretical prediction for the 2vββ-decay halflives, which were based on within closure approximation calculated Corresponding NMEs, with the measured half-lives.



J. Barea, J. Kotila, F. Iachello, PRC 87, 014315 (2013).

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Improved description of the $0\nu\beta\beta$ -decay rate (and novel approach of fixing g_A^{eff})

The g_A^{eff} can be deterimed with measured half-life and ratio of NMEs and calculated NME dominated by transitions through low lying states of the intermediate nucleus (ISM?)

The running sum of the $2\nu\beta\beta$ -decay NMEs (QRPA)





ξ_{13} tell us about importance of higher lying states of int. nucl.



E, keV

distributions of emitted electrons



New modes of the double beta decay

Double Beta Decay with emission of a single electron

A. Babič, M.I. Krivoruchenko, F.Š., arXiv:1805.07815 [hep-ph]

[Jung *et al.* (GSI), 1992] observed beta decay of ${}^{163}_{66}$ Dy⁶⁶⁺ ions with Electron Production (EP) in K or L shells: $T_{1/2}^{EP} = 47$ d

Bound-state double-beta decay $0\nu EP\beta^-$ ($2\nu EP\beta^-$) with EP in available $s_{1/2}$ or $p_{1/2}$ subshell of daughter 2+ ion:



Search for possible manifestation in single-electron spectra...



Single-electron spectra for ${}^{82}Se$ (Q = 2.998 MeV):

Bound- and free-electron Fermi functions: $B_n(Z,A) = f_{n,-1}^2(R) + g_{n,+1}^2(R)$ $F(Z,E) = f_{-1}^2(R,E) + g_{+1}^2(R,E)$ Relativistic electron wave functions in central field:

$$\psi_{\kappa\mu}(\vec{r}) = \begin{pmatrix} f_{\kappa}(r) \,\Omega_{\kappa\mu}(\hat{r}) \\ ig_{\kappa}(r) \,\Omega_{-\kappa\mu}(\hat{r}) \end{pmatrix}$$

$$\kappa = (l - j)(2j + 1) = \pm 1, \pm 2, \dots$$

$$j = |l \pm 1/2| \qquad \mu = -j, \dots, +j \qquad 54$$

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Fedor Simkovic

CALCULATION: GRASP2K

Stationary *N*-particle Dirac eq. with separable central atomic Hamiltonian [a.u.]:

$$\begin{aligned} \left| \sum_{i=1}^{N} -i\nabla_{i} \cdot \vec{\alpha}c + \beta c^{2} - \frac{Z}{r_{i}} + V(r_{i}) \right| \Psi &= E \Psi \\ \Psi &= \frac{1}{\sqrt{N!}} \begin{vmatrix} \psi_{1}(\vec{r}_{1}) & \cdots & \psi_{1}(\vec{r}_{N}) \\ \vdots & \ddots & \vdots \\ \psi_{N}(\vec{r}_{1}) & \cdots & \psi_{N}(\vec{r}_{N}) \end{vmatrix} \end{aligned}$$

Multiconfiguration Dirac–Hartree–Fock package GRASP2K:

- Fit of non-convergent orbitals: $f_{n,-1}^2$, $g_{n,+1}^2(R) \approx aZ^b$
- Fit of orbitals beyond n = 9: $f_{n,-1}^2, g_{n,+1}^2(R) \approx cn^d$



$0\nu EP\beta^{-}$ Single-Electron Spectrum (⁸²Se)

 $0\nu\beta^{-}\beta^{-}$ and $0\nu EP\beta^{-}$ single-electron spectra $1/\Gamma^{0\nu\beta\beta} d\Gamma/dE$ vs. electron kinetic energy $E - m_e$ for ⁸²Se (Q = 2.996 MeV)



 $E - m_e$ [MeV]

$0\nu EP\beta^-$ Half-Lives

 $0\nu\beta^{-}\beta^{-}$ and $0\nu EP\beta^{-}$ half-lives $T_{1/2}^{0\nu\beta\beta}$ and $T_{1/2}^{0\nu EP\beta}$ estimated for $\beta^{-}\beta^{-}$ isotopes with known NME $|M^{0\nu\beta\beta}|$, assuming unquenched $g_{A} = 1.269$ and $|m_{\beta\beta}| = 50$ meV



$2\nu EP\beta^{-}$ Single-Electron Spectrum (⁸²Se)

 $2\nu\beta^{-}\beta^{-}$ and $2\nu EP\beta^{-}$ single-electron spectra $1/\Gamma d\Gamma/dE$ vs. electron kinetic energy $E - m_e$ for ⁸²Se (Q = 2.996 MeV)



 $E - m_e$ [MeV]

$2\nu EP\beta^-$ Half-Lives predictions (independent on g_A and value of NME)

 $2\nu\beta^{-}\beta^{-}$ and $2\nu EP\beta^{-}$ half-lives $T_{1/2}^{2\nu\beta\beta}$ and $T_{1/2}^{2\nu EP\beta}$ calculated for $\beta^{-}\beta^{-}$ isotopes observed experimentally, assuming unquenched $g_{A} = 1.269$



DBD theoretical challengies

Particle physics:

- 1. Understanding of the effective Majorana mass
- 2. What is the dominant mechanism of the $0\nu\beta\beta$ -decay
- 3. Connection to laboratory v-mass measurement, cosmology LHC physics, etc

Nuclear physics:

1. Progress in nuclear structure theory

reliable description of the β-, EC-, 2νββ-decay, ChER, DCX etc role of the isospin and spin-isospin symmetry understanding of uncertainty in calculated NMEs

2. Understanding of quenching of g_A

Instead of Conclusions

LHC physics

 $rac{1}{\Lambda^2}\sum_i c_i^{(6)}\mathcal{O}_i^{(6)} + O(rac{1}{\Lambda^3})$







Progress in nuclear structure calculations is highly required

We are at the beginning of the Beyond Standard Model Road...



The future of neutrino physics is bright

