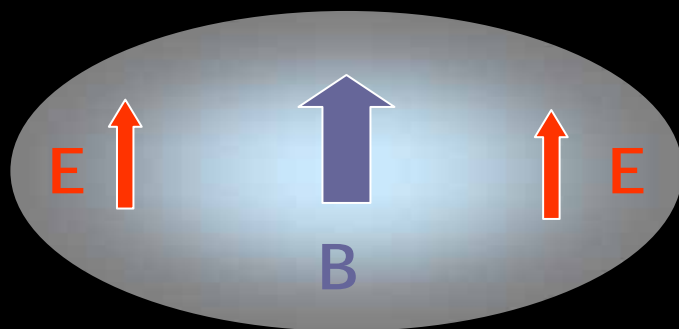




Strong CP Violation & Magnetic Fields

- Prepared for QCD@work2007 -



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& Raffaele Millo

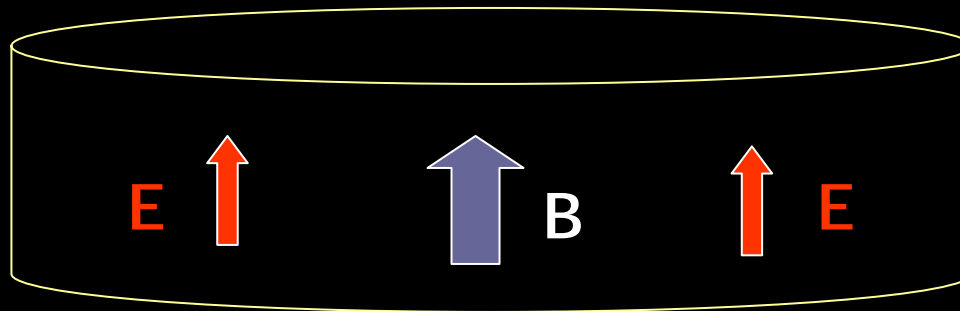
(Trento)

Reference: R. Millo and P. Faccioli ArXiv: 0706.0805 (hep)

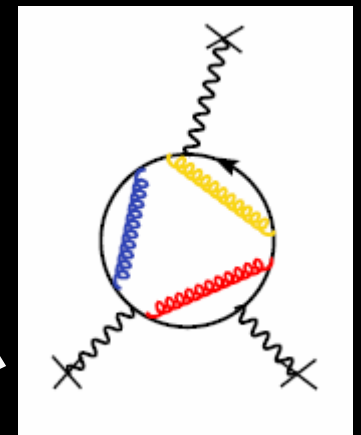
The main point of this talk:

Question: what happens to the QCD theta-vacuum in the presence of external magnetic fields?

Solenoid



CP-odd effect



$$S_{\theta} = \frac{\theta}{32\pi^2} \int d^4x G_{\mu\nu} \tilde{G}^{\mu\nu}$$

Why bother?

Primordial magnetic fields

Universe is permeated by large-scale magnetic fields:

- * Strength: $\sim \mu\text{G}$
- * Correlation length: $\sim 30 \text{ kpc}$

What is the origin of such fields? Two main hypothesis

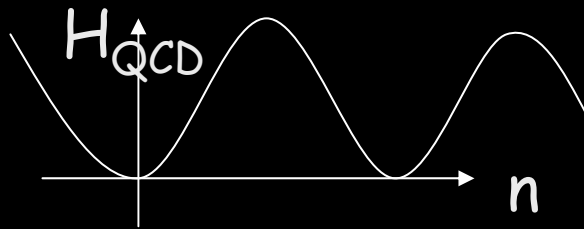
- * **Primordial**
- * Astrophysical (i.e. after galaxy formation)

Induced Vacuum Electric Dipole Moment


Starting point: induced polarization in the QCD vacuum:

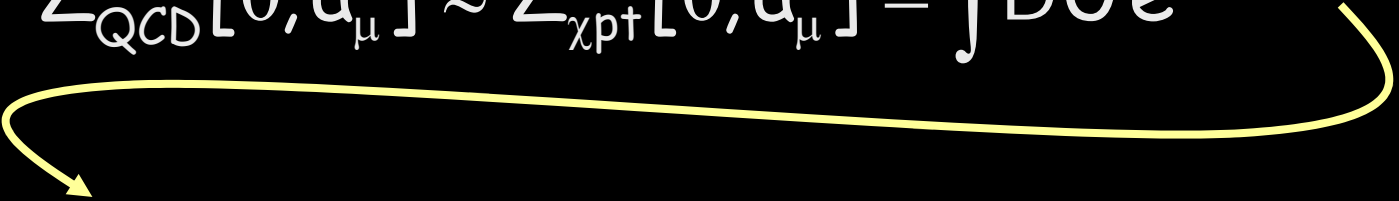
$$p_z = \frac{1}{V} \int d^3r r_z \rho(r)$$

$$\rho(r) = \langle \theta | J_0(r) | \theta \rangle_{A_\mu^{\text{ext}}} \quad | \theta \rangle = \sum_n e^{in\theta} | n \rangle$$



Calculation of the VEDM

$$\langle \theta | J_0(x) | \theta \rangle_{A_\mu^{\text{ext}}} = \left(\frac{\delta}{\delta i a_\mu(x)} Z_{\text{QCD}}[\theta, a_\mu] \right)_{a_\mu = A_\mu^{\text{ext}}}$$


$$Z_{\text{QCD}}[\theta, a_\mu] \approx Z_{\chi \text{pt}}[\theta, a_\mu] = \int D U e^{i \int dt L_{\chi \text{pt}}[a_\mu, \theta]}$$


$$L_{\chi \text{pt}} = L^{(2)}_{\chi \text{pt}}[a_\mu] + L^{(4)}_{\chi \text{pt}}[a_\mu] + L_{\text{anom.}}[\theta]$$

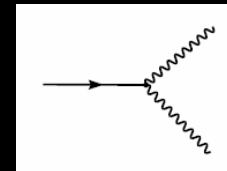
The role of the anomaly (1)

Chiral and axial anomalies are crucial for this effect.

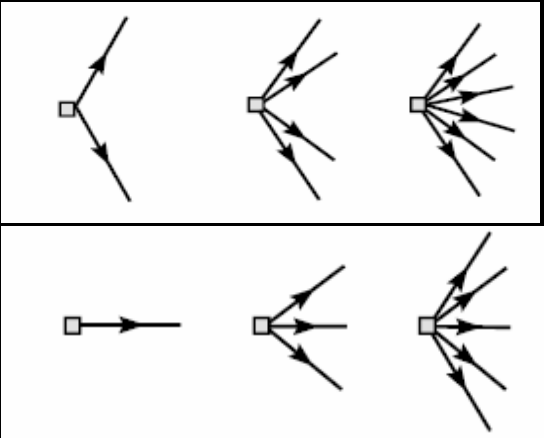
* The **axial anomaly** enters, to leading $1/N_c$ through

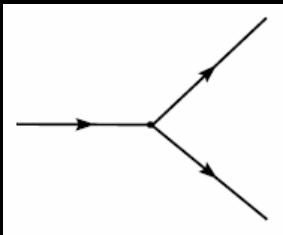
$$\mathcal{L}_{\text{anom}}[\theta] = -\frac{f_\pi^2 a}{4N_c} \left(\frac{i}{2} \log \left[\frac{\det U}{\det U^\dagger} \right] - \theta \right)$$

* The **chiral anom.** enter through the Wess-Zumino coupling in $\mathcal{L}_{\chi\text{pt}}^{(4)}$ (which accounts for $\pi \rightarrow \gamma \gamma$):



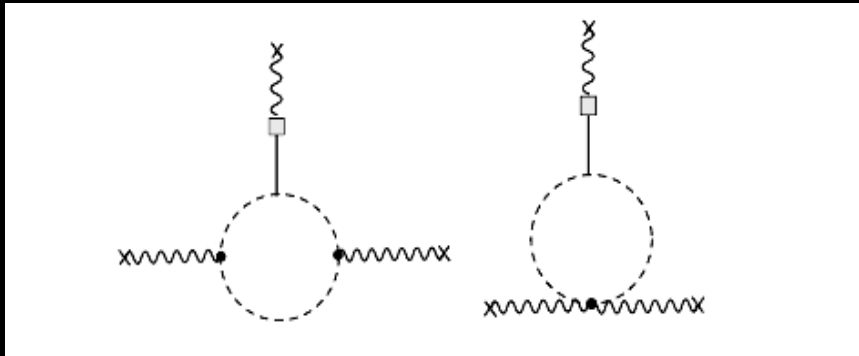
The role of the anomaly (2)

$$J_{\mu}^{e/m}(x) = \frac{\delta L[a_{\mu}, \theta]}{\delta a_{\mu}(x)} = \left\{ \begin{array}{ll} \text{non-anom.} \\ \text{anom. (WZ)} \end{array} \right.$$


$$L_{\text{anom}}[\theta] =$$


CP-odd diagrams must include the chiral anomaly through the Wess-Zumino e/m coupling to photons

Magnetically-induced VEDM



For an external magnetic field:

$$\vec{B} = (0, 0, B_0 \cos \bar{\omega} t)$$

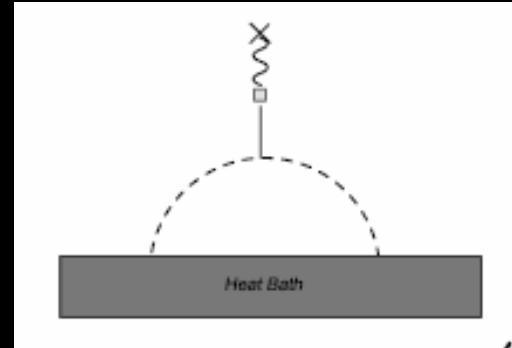
$$p_z(t) \approx -\theta \alpha^2 \frac{5\pi}{36} \frac{B_0^3}{f_\pi^2 m_\eta^4} \bar{\omega}^2 (\cos \bar{\omega} t - \cos 3\bar{\omega} t)$$

- Note:
- * Two characteristic response modes
 - * Polariz. vanishes for $\omega \rightarrow 0$ (energy cons.)
 - * Result is param. free (leading order & $1/N_c$)

Vacuum polarization by primordial magnetic fields

Repeat calculation
at $T > 0$:

$$(0 < T \ll 4\pi f_\pi)$$

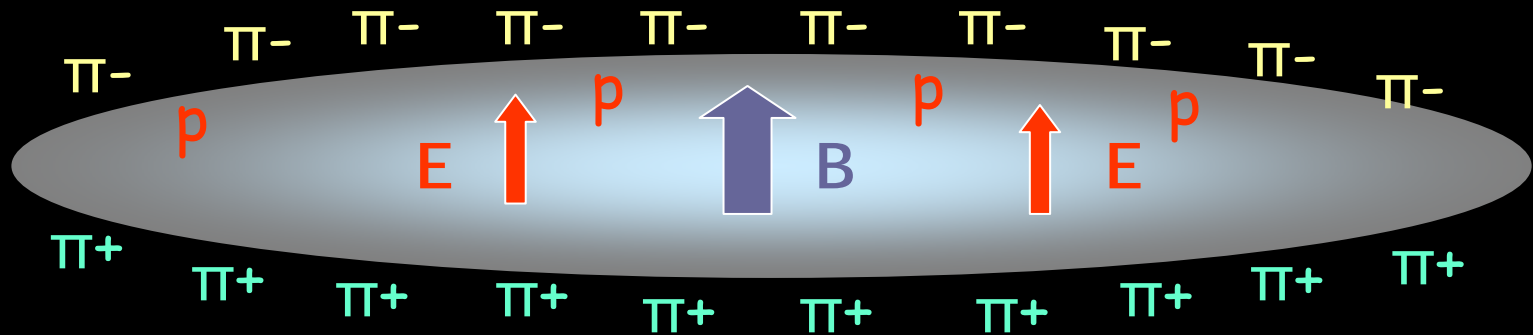


$$p_z \approx \theta\alpha \frac{25B_0}{24\pi} \frac{m_\pi^2}{f_\pi^2 m_\eta^2} \int \frac{d^3p}{(2\pi)^3} \frac{1}{2\omega} \frac{1}{e^{\frac{\omega}{T}} - 1}$$

Note: * $T > 0$ static B can polarize the vacuum
* $\mathcal{O}(\theta\alpha)$ rather than $\mathcal{O}(\theta\alpha^2)$

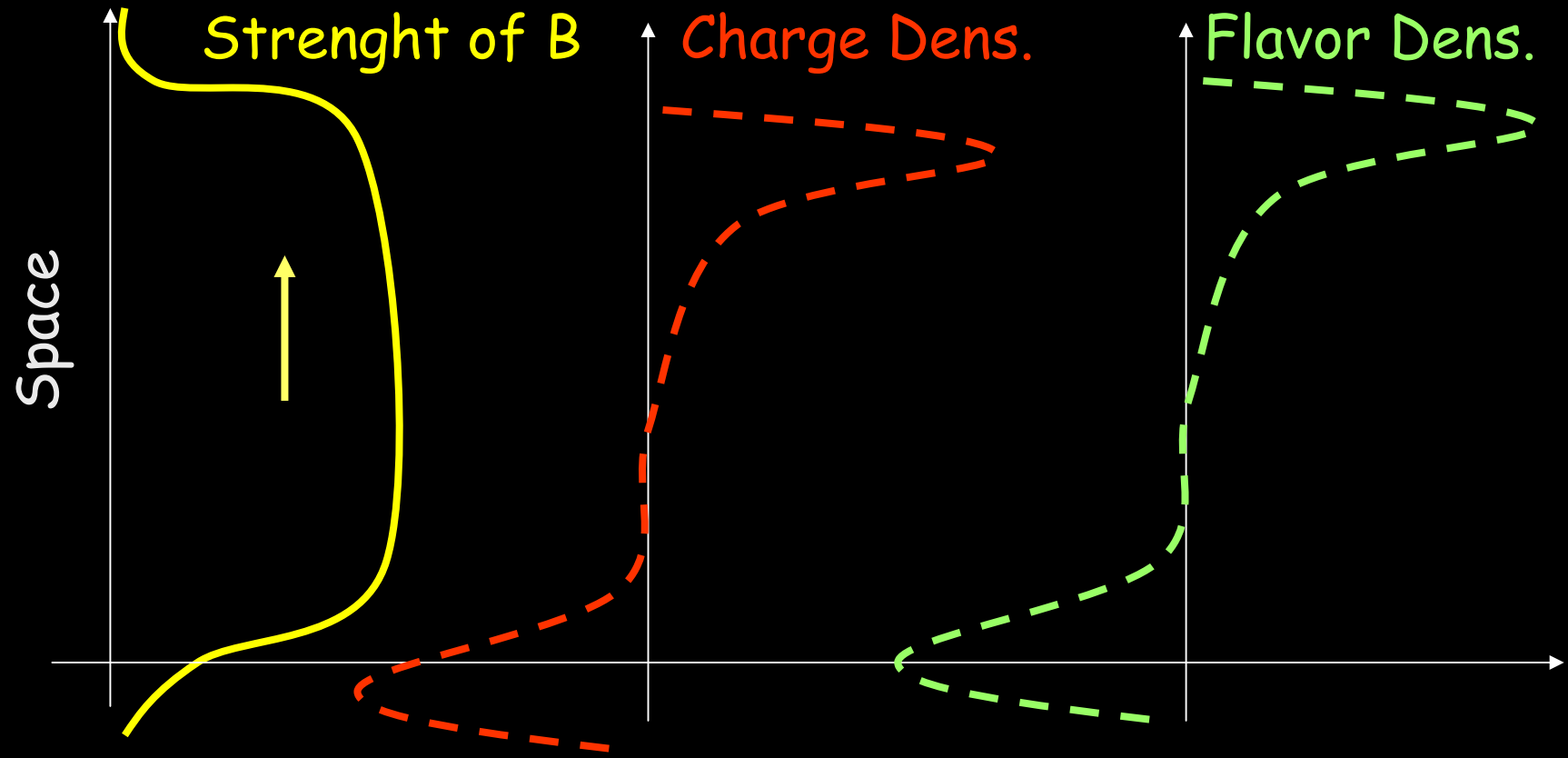
Linking primordial magnetic fields and strong CP violations

Strong interaction were
CP-violating at the end at the hadronic epoch,
then primordial magnetic fields must have induced
a macroscopic (astrophysical) separation of electric
charge and flavor



NB:CP-odd effect!

Charge & flavor profiles in the primordial magnetic domains



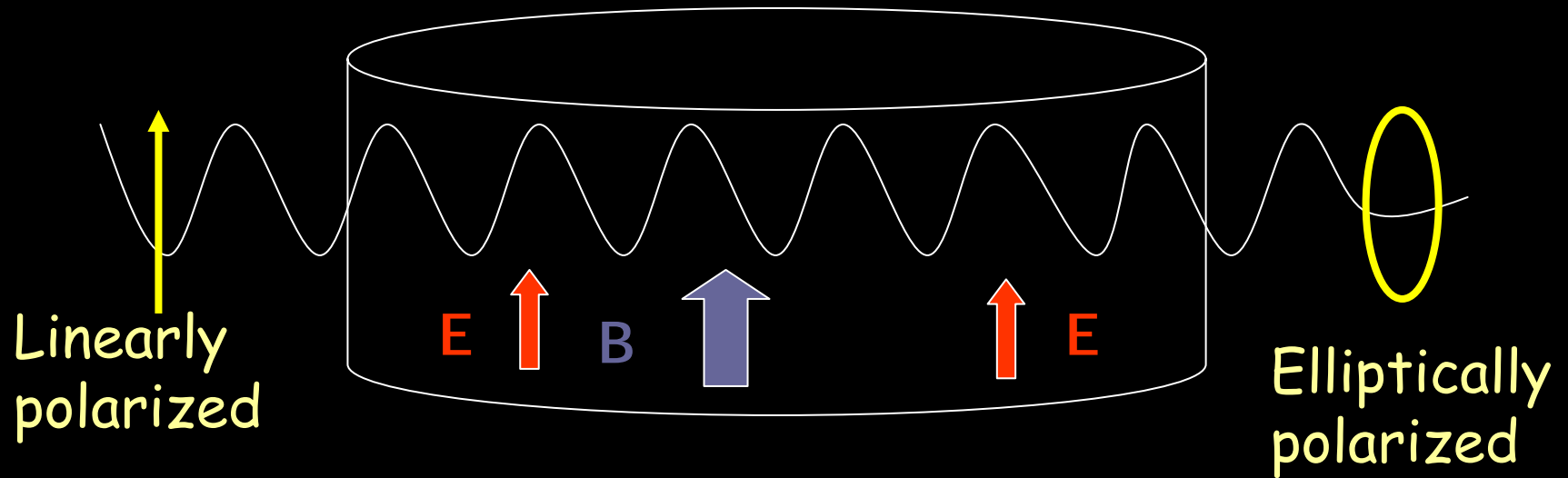
Consequences:

The fate of the charge separation depends on the details of the subsequent stages of the expansion

When T or θ became sufficiently small after the end of the hadronic epoch, we expect large annihilation events.

The resulting low-energy γ -rays would be visible only if the annihilation took place after the decoupling of matter and radiation. What signatures? What consequences?

Future direction: PVLAS experiment



Can we explain the induced ellipticity without having to invoke axions? -Work in progress-

Conclusions

Magnetic fields
+ CP violation



flavor (charge) asymmetry
over macroscopic distance
scales

Ch.pt
+ 1/Nc

$$\left\{ \begin{array}{ll} p_z(t) \approx -\theta\alpha^2 \frac{5\pi}{36} \frac{B_0^3}{f_\pi^2 m_\eta^4} \bar{\omega}^2 (\cos \bar{\omega} t - \cos 3\bar{\omega} t) & T=0 \\ p_z \approx \theta\alpha \frac{25B_0}{24\pi} \frac{m_\pi^2}{f_\pi^2 m_\eta^2} \int \frac{d^3p}{(2\pi)^3} \frac{1}{2\omega} \frac{1}{e^{\frac{\omega}{T}} - 1} & T>0 \end{array} \right.$$

- * Cosmological Consequences?
- * Experimental consequences (PVLAS)?